

# JEE Main – 2025

# 24<sup>th</sup> JANUARY 2025 (Evening Shift)

# **General Instructions**

- 1. The test is of **3 hours** duration and the maximum marks is **300**.
- The question paper consists of 3 Subjects (Subject I: Mathematics, Subject II: Physics, Subject III: Chemistry).
   Each Part has two sections (Section 1 & Section 2).
- **3.** Section 1 contains 20 Multiple Choice Questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE CHOICE is correct.
- **4. Section 2** contains **5 Numerical Value Type Questions**. The answer to each question is an **integer** ranging from 0 to 999.
- 5. No candidate is allowed to carry any textual material, printed or written, bits of papers, pager, mobile phone, any electronic device, etc. inside the examination room/hall.
- 6. On completion of the test, the candidate must hand over the Answer Sheet to the **Invigilator** on duty in the Room/Hall. **However, the candidates are allowed to take away this Test Booklet with them**.

# Marking Scheme

- **1. Section 1:** +4 for correct answer, –1 (negative marking) for incorrect answer, 0 for all other cases.
- 2. Section 2: +4 for correct answer, –1 (negative marking) for incorrect answer, 0 for all other cases.

| SU         | BJECT     | I: MATHER   | MATICS                      |                              |                |                             |                                       | <b>MARKS: 100</b>                                       |  |
|------------|-----------|---|-----------------------------|------------------------------|----------------|-----------------------------|---------------------------------------|---|--|
|            |           |   |                             | SE                           | CTION-         | L                           |                                       | ;   |  |
| This :     | section c | ontains 20 Mi   | ultiple Choi                | e Questions.                 | Each quest     | ion has 4 c                 | hoices (1), (2)                       | ), (3) and (4), out of whic                             |  |
| ONLY       | ONE CH    | OICE is correc  | t.                          |                              |                |                             |                                       |   |  |
| 1.         |           | the function  |                             | 0                            |                | -                           | •                                     | e numbers of the points, ferentiable. Then $m + n$ is   |  |
|            | (1)       | 9   | (2)                         | 8                            | (3)            | 6                           | (4)                                   | 7   |  |
| 2.         | In an     | arithmetic pr   | ogression, i                | f $S_{40} = 1030$            | and $S_{12} =$ | 57 , then $S$               | <sub>30</sub> – S <sub>10</sub> is eq | jual to:  |  |
|            | (1)       | 515   | (2)                         | 525                          | (3)            | 510                         | (4)                                   | 505   |  |
| 3.         | Let (2    | , 3) be the la  | argest open                 | interval in w                | hich the fu    | unction $f(x)$              | $z = 2 \log_e(x - x)$                 | 2) – $x^2$ + $ax$ +1 is strictly                        |  |
|            |           | asing and ( <i>b,</i><br>y decreasing.  |                             |                              |                | which the                   | e function g(                         | $(x) = (x-1)^3(x+2-a)^2$ is                             |  |
|            | (1)       | 420   | (2)                         | 160                          | (3)            | 280                         | (4)                                   | 360   |  |
| <b>1</b> . | The n     | umber of real   | solution(s)                 | of the equatio               | on $x^2 + 3x$  | $+2 = \min\left\{ z\right $ | x-3 ,  x+2                            | is :  |  |
|            | (1)       | 0   | (2)                         | 1                            | (3)            | 3                           | (4)                                   | 2   |  |
| 5.         | The e     | The equation of the chord, of the ellipse $\frac{x^2}{25} + \frac{y^2}{16} = 1$ , whose mid-point is (3, 1) is: |                             |                              |                |                             |                                       |   |  |
|            | (1)       | 5x + 16y =  | 31                          |                              | (2)            | <b>2)</b> $48x + 25y = 169$ |                                       |   |  |
|            | (3)       | 4x + 122y   | = 134                       |                              | (4)            | 25x + 10                    | 1 <i>y</i> = 176                      |   |  |
| 3.         | If 7 =    | $5+\frac{1}{7}(5+\alpha)+$  | $\frac{1}{7^2}(5+2\alpha)$  | $-\frac{1}{7^3}(5+3\alpha)+$ | ∞, then        | the value of                | ofα is:                               |   |  |
|            | (1)       | 1   | (2)                         | $\frac{1}{7}$                | (3)            | $\frac{6}{7}$               | (4)                                   | 6   |  |
| 7.         | Let th    | the points $\left(\frac{11}{2}\right)$  | $, \alpha $ lie on $\alpha$ | or inside the t              | riangle wit    | n sides $x$ +               | y = 11, x + 2y                        | y = 16  and  2x + 3y = 29,                              |  |
|            | Then      | the product o   | of the smalle               | st and the lar               | gest values    | of $\alpha$ is equ          | ual to :                              |   |  |
|            | (1)       | 44  | (2)                         | 33                           | (3)            | 55                          | (4)                                   | 22  |  |
| 3.         | ways,     |   | girls can b                 | -                            |                |                             | -                                     | d 5 girls. The number of oup <i>A</i> and the remaining |  |
|            | (1)       | 8925  | (2)                         | 8575                         | (3)            | 9100                        | (4)                                   | 8750  |  |
| ).         | Let $f$   | : $(0,\infty) \to \mathbf{R}$   | be a functi                 | on which is                  | differential   | ole at all p                | oints of its d                        | lomain and satisfies the                                |  |
|            | condi     | tion $x^2 f'(x)$ =  | =2xf(x)+3,                  | with $f(1) = 4$              | . Then $2f$    | 2) is equal                 | to:                                   |   |  |
|            | (1)       | 23  | (2)                         | 29                           | (3)            | 19                          | (4)                                   | 39  |  |

| 10. | Let $A = \begin{bmatrix} a_{ij} \end{bmatrix}$ be a square matrix of order 2 with entries either 0 or 1. Let <i>E</i> be the event that <i>A</i> is an |   |  |  |   |  |                     |  |
|-----|--|---|--|--|---|--|---------------------|--|
|     | invertible matrix. Then the probability $P(E)$ is :  |   |  |  |   |  |                     |  |
|     | (1)  | $\frac{3}{16}$  | (2)  | $\frac{3}{8}$  | (3)   | $\frac{5}{8}$                              | (4)                 | $\frac{1}{8}$                            |
| 11. | Let a  | $=3\hat{i}-\hat{j}+2\hat{k}$ , $ec{b}=$                                 | $= \vec{a} \times (\hat{i} - $                 | $2\hat{k}$ ) and $\vec{c} = \vec{b} \times \vec{b}$  | k. Then t                                       | the projection of                          | $ec{c}-2\hat{j}$ (  | on $\vec{a}$ is:                         |
|     | (1)  | $2\sqrt{7}$   | (2)  | $2\sqrt{14}$   | (3)   | $\sqrt{14}$                                | (4)                 | $3\sqrt{7}$                              |
| 12. | Suppo  | se A and B are  | the coe  | fficients of 30th a  | and $12^{	ext{th}}$                             | terms respective                           | ely in th           | e binomial expansion of                  |
|     | $(1+x)^{2}$  | $^{2n-1}$ . If $2A = 5B$  | , then <i>n</i>                                | is equal to:   |   |  |                     |  |
|     | (1)  | 22  | (2)  | 21   | (3)   | 19   | (4)                 | 20                                       |
| 13. | If the   | e equation of   | the  | parabola with  | vertex  | $V\left(\frac{3}{2},3\right)$ and          | the o               | directrix $x + 2y = 0$ is                |
|     | $\alpha x^2 +$   | $\beta y^2 - \gamma xy - 30x -$   | -60 <i>y</i> +2                                | $225 = 0$ , then $\alpha$ -  | $+\beta +\gamma$ is                             | equal to:                                  |                     |  |
|     | (1)  | 8   | (2)  | 6  | (3)   | 7  | (4)                 | 9  |
| 14. | The ar   | rea of the region   | enclosed                                       | d by the curves g  | $y = e^{X}, y$                                  | $= e^{x}-1 $ and y-                        | axis is:            |  |
|     | (1)  | $1 + \log_e 2$  | (2)  | $\log_e 2$   | (3)   | $2\log_e 2 - 1$                            | (4)                 | $1 - \log_e 2$                           |
| 15. | Let A  | $= \left\{ x \in (0,\pi) - \left\{ \frac{\pi}{2} \right\} \right\}$     | : log <sub>(2/</sub>                           | $ \sin x  + \log_{(2/2)}$  | $_{\pi)} \cos x $                               | =2 and                                     |                     |  |
|     | $B = \left\{ x \right\}$   | $x \ge 0: \sqrt{x}(\sqrt{x}-4)$   | $-3 \sqrt{x}$                                  | -2 +6=0. The   | $n n(A \cup$                                    | <i>B</i> ) is equal to:                    |                     |  |
|     | (1)  | 2   | (2)  | 4  | (3)   | 8  | (4)                 | 6  |
| 16. | If the s   | system of equation  | ons  |  |   |  |                     |  |
|     | x + 2y   | -3z = 2   |  |  |   |  |                     |  |
|     | $2x + \lambda$   | y + 5z = 5  |  |  |   |  |                     |  |
|     | 14x + 3  | $3y + \mu z = 33$   |  |  |   |  |                     |  |
|     | has in   | finitely many sol   | utions,  | then $\lambda + \mu$ is equ  | ual to :  |  |                     |  |
|     | (1)  | 10  | (2)  | 13   | (3)   | 11   | (4)                 | 12                                       |
|     |  |   | $a + \frac{s}{s}$                              | $\frac{\sin x}{x}$ 1   | b   |  |                     |  |
| 17. | For so   | me $a, b, let f(x)$   | ) = 0  | $a \qquad 1 + \frac{\sin x}{1 - \frac$ | b   | $x \neq 0$ , lim $f(x)$                    | $= \lambda + \mu a$ | + vb. Then $(\lambda + \mu + v)^2$ is    |
|     |  |   |  | x<br>1   | $h + \frac{\sin x}{2}$                          | $x \rightarrow 0$                          | ·                   | + $vb$ . Then $(\lambda + \mu + v)^2$ is |
|     |  |   |  | ~ 1  | x   |  |                     |  |
|     | equal 1<br>(1)   | 36  | (2)  | 16   | (3)   | 25   | (4)                 | 9  |
| 18. |  | $\beta > \gamma > 0$ , then th  |  |  | (3)   | 20   | (4)                 | 9  |
|     |  | ( - )   | -  | - ) (  | (1  | 2)   |                     |  |
|     | $\cot^{-1}$  | $\left\{\beta + \frac{(1+\beta^{-})}{(\alpha-\beta)}\right\} + co^{-1}$ | $t^{-1} \left\{ \gamma + \frac{1}{2} \right\}$ | $\frac{(1+\gamma^2)}{(\beta-\gamma)} \right\} + \cot^{-1} \left\{ -\frac{1}{2} \right\}$   | $\alpha + \frac{(1+\alpha)}{(\gamma - \alpha)}$ | $\left. \frac{J}{J} \right\}$ is equal to: |                     |  |
|     | (1)  | π   | (2)  | $\frac{\pi}{2} - (\alpha + \beta + \gamma)$  | (3)   | 0  | (4)                 | 3π                                       |

- **19.** Let the position vectors of three vertices of a triangle be  $4\vec{p} + \vec{q} 3\vec{r}, -5\vec{p} + \vec{q} + 2\vec{r}$  and  $2\vec{p} \vec{q} + 2\vec{r}$ . If the position vectors of the orthocenter and the circumcenter of the triangle are  $\frac{\vec{p} + \vec{q} + \vec{r}}{4}$  and  $\alpha \vec{p} + \beta \vec{q} + \gamma \vec{r}$  respectively, then  $\alpha + 2\beta + 5\gamma$  is equal to:
  - (1) 1 (2) 3 (3) 4 (4) 6

**20.** The function 
$$f: (-\infty, \infty) \to (-\infty, 1)$$
, defined by  $f(x) = \frac{2^{x} - 2^{-x}}{2^{x} + 2^{-x}}$  is:

(1)

- One-one but not onto (2) Both one-one and onto
- (3) Onto but not one-one (4) Neither one-one nor onto

## SECTION-2

This section contains Five (05) Numerical Value Type Questions. The answer to each question is an integer ranging from 0 to 999.

- Let P be the image of the point Q(7, -2, 5) in the line  $L: \frac{x-1}{2} = \frac{y+1}{3} = \frac{z}{4}$  and R(5, p, q) be a point on L. 21. Then the square of the area of  $\triangle PQR$  is \_\_\_\_\_.
- Let y = y(x) be the solution of the differential equation  $2\cos x \frac{dy}{dx} = \sin 2x 4y \sin x, x \in \left(0, \frac{\pi}{2}\right)$ . If 22.  $y\left(\frac{\pi}{3}\right) = 0$ , then  $y'\left(\frac{\pi}{4}\right) + y\left(\frac{\pi}{4}\right)$  is equal to \_\_\_\_\_.
- 23. Number of functions  $f: \{1, 2, ..., 100\} \rightarrow \{0, 1\}$ , that assign 1 to exactly one of the positive integers less than or equal to 98, is equal to \_\_\_\_\_\_
- Let  $H_1: \frac{x^2}{a^2} \frac{y^2}{b^2} = 1$  and  $H_2: -\frac{x^2}{a^2} + \frac{y^2}{B^2} = 1$  be two hyperbolas having length of latus rectums  $15\sqrt{2}$ 24. and  $12\sqrt{5}$  respectively. Let their ecentricities be  $e_1 = \sqrt{\frac{5}{2}}$  and  $e_2$  respectively. If the product of the lengths of their transverse axes is  $100\sqrt{10}$ , then  $25e_2^2$  is equal to \_\_\_\_\_.

25. If 
$$\int \frac{2x^2 + 5x + 9}{\sqrt{x^2 + x + 1}} dx = x\sqrt{x^2 + x + 1} + \alpha\sqrt{x^2 + x + 1} + \beta \log_e \left| x + \frac{1}{2} + \sqrt{x^2 + x + 1} \right| + C$$
, where *C* is the constant of integration, then  $\alpha + 2\beta$  is equal to

of integration, then  $\alpha + 2\beta$  is equal to \_

# **SUBJECT II: PHYSICS**

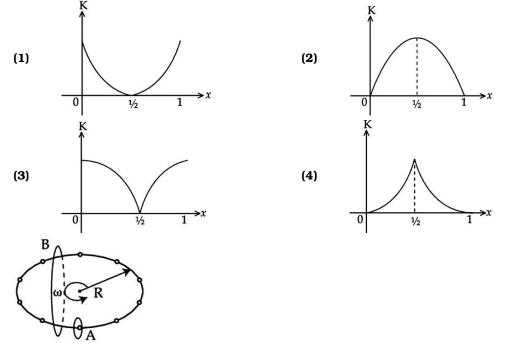
# **MARKS: 100**

# **SECTION-1**

This section contains 20 Multiple Choice Questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE CHOICE is correct.

**26.** A particle oscillates along the *x*-axis according to the law,  $x(t) - x_0 \sin^2\left(\frac{t}{2}\right)$  where  $x_0 = 1m$ . The kinetic

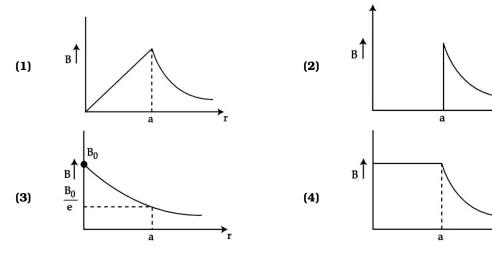
energy (K) of the particle as a function of x is correctly represented by the graph.



*N* equally spaced charges each of value q, are placed on a circle of radius *R*. The circle rotates about its axis with an angular velocity  $\omega$  as shown in the figure. A bigger Amperian loop *B* encloses the whole circle where as a smaller Amperian loop *A* encloses a small segment. The difference between enclosed currents,  $I_A - I_B$ , for the given Amperian loops is:

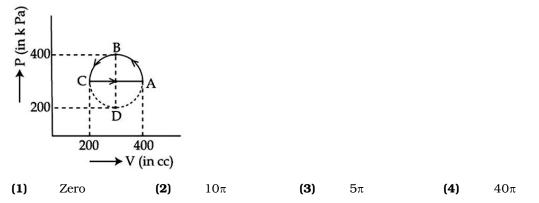
(1) 
$$\frac{2\pi}{N}q\omega$$
 (2)  $\frac{N}{\pi}q\omega$  (3)  $\frac{N}{2\pi}q\omega$  (4)  $\frac{N^2}{2\pi}q\omega$ 

**28.** A long straight wire of a circular cross-section with radius 'a' carries a steady current *I*. The current *I* is uniformly distributed across this cross-section. The plot of magnitude of magnetic field *B* with distance *r* from the centre of the wire is given by:



27.

**29.** The magnitude of heat exchanged by a system for the given cyclic process *ABCA* (as shown in figure) is (in SI unit)





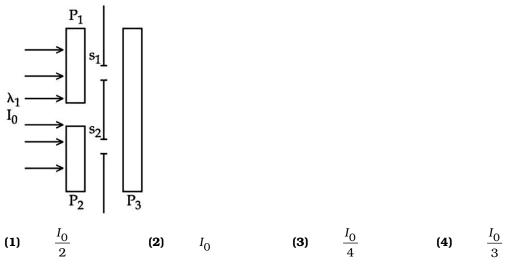
A small uncharged conducting sphere is placed in contact with an identical sphere but having  $4 \times 10^{-8}C$  charge and then removed lo a distance such that the force of repulsion between them is  $9 \times 10^{-3}N$ . The distance between them is (Take  $\frac{1}{4\pi \epsilon_0}$  as  $9 \times 10^9$  in SI units)

(1) 2 cm (2) 1 cm (3) 4 cm (4) 3 cm

**31.** The position vector of a moving body at any instant of time is given as  $\vec{r} = (5t^2\hat{i} - 5t\hat{j})m$ . The magnitude and direction of velocity at t = 2s is:

- (1)  $5\sqrt{15}$  m/s, making an angle of tan<sup>-1</sup>4 with -ve Y axis
- (2)  $5\sqrt{17}$  m/s, making an angle of  $\tan^{-1}4$  with -ve Y axis
- (3)  $5\sqrt{15}$  m/s, making an angle of  $\tan^{-1} 4$  with +ve X axis
- (4)  $5\sqrt{17}$  m/s, making an angle of tan<sup>-1</sup> 4 with +ve X axis
- **32.** In a Young's double slit experiment, three polarizers are kept as shown in the figure. The transmission axes of  $P_1$  and  $P_2$  are orthogonal to each other. The polarizer  $P_3$  covers both the slits with its transmission axis at 45° to those of  $P_1$  and  $P_2$ . An unpolarized light of wavelength  $\lambda$  and intensity  $I_0$  is incident on  $P_1$  and  $P_2$ . The intensity at a point after  $P_3$  where the path difference between the light  $\lambda$

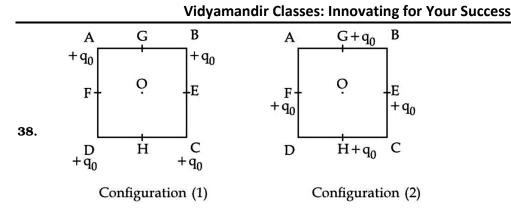
waves from 
$$s_1$$
 and  $s_2$  is  $\frac{\lambda}{3}$ , is:



|    |  | V  | iayama            | ndir Classes: I  | nnovatii   | ig for Your Su                      | ccess               |                                       |  |  |
|----|--|--|-------------------|------------------|------------|-------------------------------------|---------------------|---------------------------------------|--|--|
| 3. | In pho   | In photoelectric effect, the stopping potential $(V_0)v/s$ frequency $(v)$ curve is plotted.                   |                   |                  |            |                                     |                     |                                       |  |  |
|    | (h is t  | ( <i>h</i> is the Planck's constant and $\phi_0$ is work function of metal)                                    |                   |                  |            |                                     |                     |                                       |  |  |
|    | (A)  | V <sub>0</sub> v/sv is li  | near              |                  |            |                                     |                     |                                       |  |  |
|    | (B)  | The slope of $V_0$ v/s v curve $=\frac{\phi_0}{h}$   |                   |                  |            |                                     |                     |                                       |  |  |
|    | (C)  | <i>h</i> constant is related to the slope of $V_0$ v/s v line  |                   |                  |            |                                     |                     |                                       |  |  |
|    | (D)  | (D) The value of electric charge of electron is not required to determine <i>h</i> using the $V_0$ v/s v curve |                   |                  |            |                                     |                     |                                       |  |  |
|    | (E)  | (E) The work function can be estimated without knowing the value of <i>h</i> .                                 |                   |                  |            |                                     |                     |                                       |  |  |
|    | Choos  | Choose the <b>correct</b> answer from the options given below:   |                   |                  |            |                                     |                     |                                       |  |  |
|    | (1)  | (A), (B) and (C  | c) only           |                  | (2)        | (D) and (E) or                      | nly                 |                                       |  |  |
|    | (3)  | (C) and (D) on   | ıly               |                  | (4)        | (A), (C) and (I                     | E) only             |                                       |  |  |
| 4. | A pho  | tograph of a lan   | dscape is         | s captured by a  | drone ca   | mera at a heigł                     | 1t of 18 k          | m. The size of the camer              |  |  |
|    |  | s 2 cm × 2 cm a<br>n the drone cam   |                   | area of the land | lscape ph  | otographed is                       | 400 km <sup>2</sup> | <sup>2</sup> . The focal length of th |  |  |
|    | (1)  | 0.9 cm   | (2)               | 1.8 cm           | (3)        | 2.8 cm                              | (4)                 | 2.5 cm                                |  |  |
| 5. | Arran  | ge the following   | in the as         | scending order o | of waveler | ıgth (λ):                           |                     |                                       |  |  |
|    | (A)  | Microwaves (2  | λ <sub>1</sub> )  |                  | (B)        | Ultraviolet ra                      | ays ( $\lambda_2$ ) |                                       |  |  |
|    | (C)  | Infrared rays  | (λ <sub>3</sub> ) |                  | (D)        | X-rays $(\lambda_4)$                |                     |                                       |  |  |
|    | Choos  | Choose the <b>most appropriate</b> answer from the options given below:  |                   |                  |            |                                     |                     |                                       |  |  |
|    | (1)  | $\lambda_4 < \lambda_3 < \lambda_1 < $   | $<\lambda_2$      |                  | (2)        | $\lambda_4 < \lambda_2 < \lambda_3$ | $<\lambda_1$        |                                       |  |  |
|    | (3)  | $\lambda_4 < \lambda_3 < \lambda_2$  | $<\lambda_1$      |                  | (4)        | $\lambda_3 < \lambda_4 < \lambda_2$ | $<\lambda_1$        |                                       |  |  |
| 6. | 5. Young's double slit interference apparatus is immersed in a liquid of refractive index 1.44, separation of 1.5 mm. The slits are illuminated by a parallel beam of light whose wavelengt 690 nm. The fringe-width on a screen placed behind the plane of slits at a distance of 0.72 m, |  |                   |                  |            | hose wavelength in air i            |                     |                                       |  |  |
|    | (1)  | 0.63 mm  | (2)               | 0.33 mm          | (3)        | 0.46 mm                             | (4)                 | 0.23 mm                               |  |  |
| 7. | The o  | utput of the circ  | uit is lov        | v (zero) for:    |            |                                     |                     |                                       |  |  |
|    | Х —<br>Ү —   | $\supset$  | -                 | $\rightarrow$    |            |                                     |                     |                                       |  |  |
|    | (A)  | X = 0, Y = 0   |                   |                  |            |                                     |                     |                                       |  |  |
|    | (B)  | X = 0, Y = 1   |                   |                  |            |                                     |                     |                                       |  |  |
|    | (C)  | X = 1, Y = 0   |                   |                  |            |                                     |                     |                                       |  |  |
|    |  | (D) $X = 1, Y = 1$   |                   |                  |            |                                     |                     |                                       |  |  |

Choose the **correct** answer from the options given below:

| (1) | (A), (B) and (C) only | (2) | (B), (C) and (D) only |
|-----|-----------------------|-----|-----------------------|
|     |                       |     |                       |



In the first configuration (1) as shown in the figure, four identical charges  $(q_0)$  are kept at the corners A, B, C and D of square of side length 'a'. In the second configuration (2), the same charges are shifted to mid points G, E, H and F, of the square. If  $K = \frac{1}{4\pi \epsilon_0}$ , the difference between the potential energies of configuration (2) and (1) is given by:

(1) 
$$\frac{Kq_0^2}{a}(4-2\sqrt{2})$$
 (2)  $\frac{Kq_0^2}{a}(4\sqrt{2}-2)$ 

(3) 
$$\frac{Kq_0^2}{a}(3-\sqrt{2})$$
 (4)  $\frac{Kq_0^2}{a}(3\sqrt{2}-2)$ 

**39.** A solid sphere is rolling without slipping on a horizontal plane. The ratio of the linear kinetic energy of the centre of mass of the sphere and rotational kinetic energy is:

(1) 
$$\frac{4}{3}$$
 (2)  $\frac{5}{2}$  (3)  $\frac{2}{5}$  (4)  $\frac{3}{4}$ 

**40.** The energy E and momentum p of a moving body of mass m are related by some equation. Given that c represents the speed of light, identify the correct equation

(1)  $E^2 = pc^2 + m^2c^2$  (2)  $E^2 = p^2c^2 + m^2c^4$ 

(3) 
$$E^2 = pc^2 + m^2 c^4$$
 (4)  $E^2 = p^2 c^2 + m^2 c^2$ 

- **41.** A solid sphere and a hollow sphere of the same mass and of same radius are rolled on an inclined plane. Let the time taken to reach the bottom by the solid sphere and the hollow sphere be  $t_1$  and  $t_2$ , respectively, then:
  - (1)  $t_1 > t_2$  (2)  $t_1 = 2t_2$

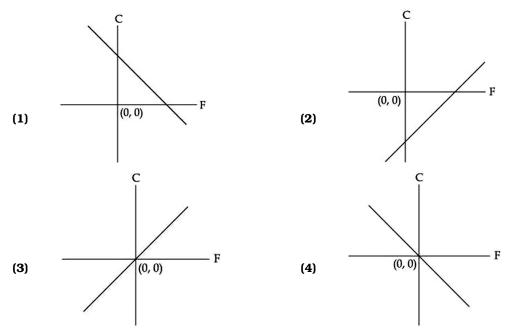
(3) 
$$t_1 = t_2$$
 (4)  $t_1 < t_2$ 

**42.** The temperature of a body in air falls from 40°C to 24°C in 4 minutes. The temperature of the air is 16°C. The temperature of the body in the next 4 minutes will be :

(1) 
$$\frac{42}{3}$$
°C (2)  $\frac{56}{3}$ °C

(3) 
$$\frac{14}{3}$$
°C (4)  $\frac{28}{3}$ °C

**43.** Which of the following figure represents the relation between Celsius and Fahrenheit temperatures?



44. Given below are two statements. One is labelled as Assertion (A) and the other is labelled as Reason (R).

**Assertion (A) :** A electron in a certain region of uniform magnetic field is moving with constant velocity in a straight line path.

**Reason (R) :** The magnetic field in that region is along the direction of velocity of the electron.

In the light of the above statements, choose the **correct** answer from the options given below :

- (1) (A) is true but (R) is false
- (2) Both (A) and (R) are true and (R) is the correct explanation of (A)
- (3) (A) is false but (R) is true
- (4) Both (A) and (R) are true but (R) is NOT the correct explanation of (A)
- 45. Given below are two statements. One is labelled as Assertion (A) and the other is labelled as Reason (R).

**Assertion (A) :** In an insulated container, a gas is adiabatically shrunk to half of its initial volume. The temperature of the gas decreases.

**Reason (R) :** Free expansion of an ideal gas is an irreversible and an adiabatic process.

In the light of the above statements, choose the **correct** answer from the options given below :

- (1) Both (A) and (R) are true but (R) is NOT the correct explanation of (A)
- (2) (A) is true but (R) is false
- (3) Both (A) and (R) are true and (R) is the correct explanation of (A)
- (4) (A) is false but (R) is true

## **SECTION-2**

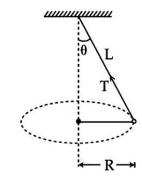
This section contains Five (05) Numerical Value Type Questions. The answer to each question is an integer ranging from 0 to 999.

**46.** A tightly wound long solenoid carries a current of 1.5 A. An electron is executing uniform circular motion inside the solenoid with a time period of 75 ns. The number of turns per metre in the solenoid is

[Take mass of electron  $m_e = 9 \times 10^{-31} kg$ , charge of electron  $|q_e| = 1.6 \times 10^{-19} C$ ,

$$\mu_0 = 4\pi \times 10^{-7} \frac{N}{A^2}, 1ns = 10^{-9} s$$

- **47.** The increase in pressure required to decrease the volume of a water sample by 0.2% is  $P \times 10^5 Nm^{-2}$ . Bulk modulus of water is  $2.15 \times 10^9 Nm^{-2}$ . The value of *P* is \_\_\_\_\_.
- **48.** Acceleration due to gravity on the surface of earth is 'g'. If the diameter of earth is reduced to one third of its original value and mass remains unchanged, then the acceleration due to gravity on the surface of the earth is \_\_\_\_\_ g.
- **49.** The ratio of the power of a light source  $S_1$  to that the light source  $S_2$  is 2.  $S_1$  is emitting  $2 \times 10^{15}$  photons per second at 600 nm. If the wavelength of the source  $S_2$  is 300 nm, then the number of photons per second emitted by  $S_2$  is \_\_\_\_\_  $\times 10^{14}$ .



50.

A string of length *L* is fixed at one end and carries a mass of *M* at the other end. The mass makes  $\left(\frac{3}{\pi}\right)$  rotations per second about the vertical axis passing through end of the string as shown. The tension in the string is *ML*.

# **SUBJECT III: CHEMISTRY**

# **MARKS: 100**

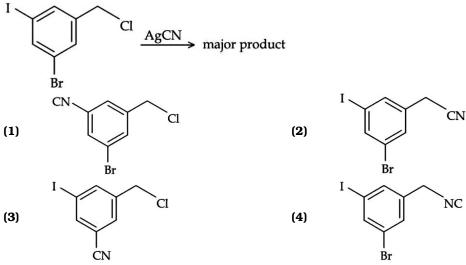
# **SECTION-1**

This section contains 20 Multiple Choice Questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE CHOICE is correct.

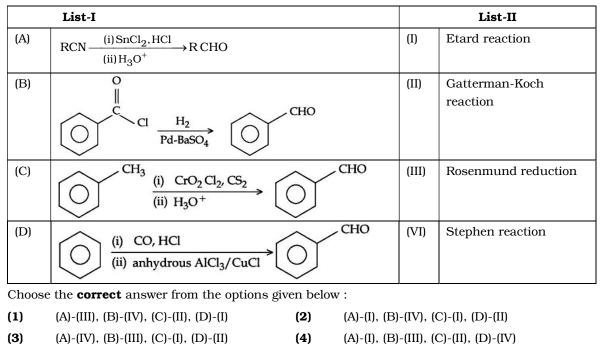
- **51.** Identify correct statement/s:
  - (A)  $-OCH_3$  and  $-NHCOCH_3$  are activating group.
  - **(B)** –CN and –OH are meta directing group.
  - (C)  $-CN \text{ and } -SO_3H$  are meta directing group.
  - **(D)** Activating groups act as ortho and para directing groups.
  - **(E)** Halides are activating groups.

Choose the **correct** answer from the options given below :

- (1) (A), (B) and (E) only (2) (A), only
- (3) (A), (C) and (D) only (4) (A) and (C) only
- **52.** The structure of the major product formed in the following reaction is :



**53.** Match **List-I** with **List-II**.



|     | List-I   | List-II                                  |
|-----|----------|--|
| (A) | Adenine  |  |
| (B) | Cytosine | (II) H <sub>3</sub> C NH<br>NH<br>H      |
| (C) | Thymine  | (III) NH <sub>2</sub><br>N N<br>N N<br>H |
| (D) | Uracil   | (VI) NH <sub>2</sub><br>N<br>N<br>H      |

#### **54.** Match **List-I** with **List-II**.

Choose the **correct** answer from the options given below :

| (1) | (A)-(IV), (B)-(III), (C)-(II), (D)-(I) | (2) | (A)-(III), (B)-(IV), (C)-(II), (D)-(I) |
|-----|--|-----|--|
| (3) | (A)-(III), (B)-(I), (C)-(IV), (D)-(II) | (4) | (A)-(III), (B)-(IV), (C)-(I), (D)-(II) |

### **55.** Given below are two statements :

**Statement (I)**: Experimentally determined oxygen-oxygen bond lengths in the  $O_3$  are found to be same and the bond length is greater than that of a O = O (double bond) but less than that of a single (O – O) bond.

**Statement (II) :** The strong lone pair-lone pair repulsion between oxygen atoms is solely responsible for the fact that the bond length in ozone is smaller than that of a double bond (O = O) but more than that of a single bond (O = O).

In the light of the above statements, choose the **correct** answer from the options given below:

- (1) Both **Statement I** and **Statement II** are false.
- (2) Both **Statement I** and **Statement II** are true.
- (3) **Statement I** is false but **Statement II** is true.
- (4) **Statement I** is true but **Statement II** is false.

56.

The elemental composition of a compound is 54.2% C, 9.2% H and 36.6% O. If the molar mass of the compound is  $132 \,\mathrm{g}\,\mathrm{mol}^{-1}$ , the molecular formula of the compound is:

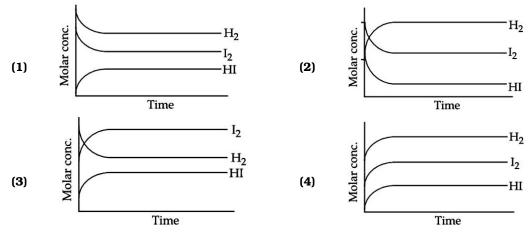
[Given: The relative atomic mass of C : H : O = 12 : 1 : 16]

(1)  $C_4H_8O_2$  (2)  $C_6H_{12}O_3$  (3)  $C_4H_9O_3$  (4)  $C_6H_{12}O_6$ 

#### 57. For the reaction,

 $H_2(g) + I_2(g) \rightleftharpoons 2HI(g)$ 

Attainment of equilibrium is predicted correctly by:



The conditions and consequence that favours the  $t_{2g}^3 e_g^1$  configuration in a metal complex are : **58**.

- (1) weak field ligand, low spin complex
- weak field ligand, high spin complex
- (3) strong field ligand, low spin complex (4)
- strong field ligand, high spin complex
- Which of the following mixing of 1M base and 1M acid leads to the largest increase in temperature ? 59.

(2)

- 50 mL HCl and 20 mL NaOH (1)
- (3) 30 mL CH<sub>3</sub>COOH and 30 mL NaOH (4)
- $45~\mathrm{mL}~\mathrm{CH}_3\mathrm{COOH}$  and  $25~\mathrm{mL}~\mathrm{NaOH}$ (2)
  - 30 mL HCl and 30 mL NaOH

60. Match List-I with List-II.

| List-I |                       |                                    | List-II |  |  |  |  |
|--------|-----------------------|------------------------------------|---------|--|--|--|--|
| ť      | Transition metal ion) | (spin only magnetic moment (B.M.)) |         |  |  |  |  |
| (A)    | Ti <sup>3+</sup>      | (I)                                | 3.87    |  |  |  |  |
| (B)    | $V^{2+}$              | (II)                               | 0.00    |  |  |  |  |
| (C)    | Ni <sup>2+</sup>      | (III)                              | 1.73    |  |  |  |  |
| (D)    | $\mathrm{Sc}^{3+}$    | (VI)                               | 2.84    |  |  |  |  |

Choose the **correct** answer from the options given below :

- (2) (A)-(III), (B)-(I), (C)-(II), (D)-(IV)
- (3) (A)-(II), (B)-(IV), (C)-(I), (D)-(III)

(4) (A)-(IV), (B)-(II), (C)-(III), (D)-(I)

 $\mathrm{S}(g) + \frac{3}{2}\mathrm{O}_2(g) \to \mathrm{SO}_3(g) + 2x\,\mathrm{kcal}$ 61.

 $SO_2(g) + \frac{1}{2}O_2(g) \rightarrow SO_3(g) + y \text{ kcal}$ 

The heat of formation of  $SO_2(g)$  is given by:

(A)-(III), (B)-(I), (C)-(IV), (D)-(II)

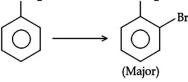
(1) 
$$y - 2x \text{ kcal}$$
 (2)  $\frac{2x}{y} \text{ kcal}$  (3)  $2x + y \text{ kcal}$  (4)  $x + y \text{ kcal}$ 

62. Find the compound 'A' from the following reaction sequences.

$$A \xrightarrow{aqua-regia} B \xrightarrow{(1) \text{KNO}_2 / \text{NH}_4 \text{OH}} \text{yellow ppt}$$
(1) MnS (2) ZnS (3) NiS (4) CoS

(1)

63. The successive 5 ionisation energies of an element are 800, 2427, 3658, 25024 and 32824 kJ/mol, respectively. By using the above values predict the group in which the above element is present:
(1) Group 2 (2) Group 4 (3) Group 14 (4) Group 13
64. For reaction
NH<sub>2</sub> NH<sub>2</sub>

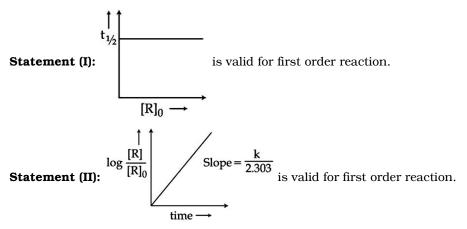


The correct order of set of reagents for the above conversion is :

- (1)  $Ac_2O, Br_2, H_2O(\Delta), NaOH$  (2)  $H_2SO_4, Ac_2O, Br_2, H_2O(\Delta), NaOH$
- (3)  $\operatorname{Br}_2 | \operatorname{FeBr}_3, \operatorname{H}_2O(\Delta), \operatorname{NaOH}$

(4) 
$$Ac_2O, H_2SO_4, Br_2, NaOH$$

**65.** Given below are two statements :



In the light of the above statements, choose the **correct** answer from the options given below :

(1) **Statement I** is true but **Statement II** is false

(2) Statement I is false but Statement II is true

(3) Both **Statement I** and **Statement II** are true

(4) Both **Statement I** and **Statement II** are false

**66.** For hydrogen atom, the orbital/s with lowest energy is/are :

(A) 4s (B)  $3p_x$  (C)  $3d_{x^2-y^2}$ 

(D)  $3d_{z^2}$  (E)  $4p_z$ 

Choose the **correct** answer from the options given below:

- (1) (A) only (2) (A) and (E) only
- (3) (B), (C) and (D) only (4) (B) only

67.

When Ethane-1,2-diamine is added progressively to an aqueous solution of Nickel (II) chloride, the sequence of colour change observed will be :

- (1) Violet  $\rightarrow$  Blue  $\rightarrow$  Pale Blue  $\rightarrow$  Green
- (2) Pale Blue  $\rightarrow$  Blue  $\rightarrow$  Violet  $\rightarrow$  Green
- (3) Green  $\rightarrow$  Pale Blue  $\rightarrow$  Blue  $\rightarrow$  Violet
- (4) Pale Blue  $\rightarrow$  Blue  $\rightarrow$  Green  $\rightarrow$  Violet

**68.** Given below are two statements :

**Statement (I)** : The first ionization energy of Pb is greater than that of Sn.

Statement (II) : The first ionization energy of Ge is greater than that of Si.

In the light of the above statements, choose the  $\mathbf{correct}$  answer from the options given below :

- (1) Both **Statement I** and **Statement II** are false
- (2) Both **Statement I** and **Statement II** are true
- (3) Statement I is false but Statement II is true
- (4) Statement I is true but Statement II is false

**69.** Based on the data given below :

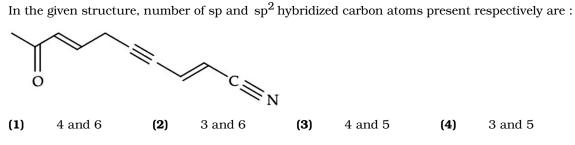
$$E^{\circ}_{Cr_2O_7^{2-}/Cr^{3+}} = 1.33V$$
  $E^{\circ}_{Cl_2/Cl^{-}} = 1.36V$ 

$$E^{\circ}_{MnO^-_4/Mn^{2+}} = 1.51\,V \quad E^{\circ}_{Cr^{3+}/Cr} = -0.74\,V$$

The strongest reducing agent is:

(1) 
$$Mn^{2+}$$
 (2)  $Cl^-$  (3)  $Cr$  (4)  $MnO_4^-$ 

**70.** In



# **SECTION-2**

This section contains Five (05) Numerical Value Type Questions. The answer to each question is an integer ranging from 0 to 999.

- **71.** The hydrocarbon (X) with molar mass 80 g mol<sup>-1</sup> and 90% carbon has \_\_\_\_\_\_ degree of unsaturation.
- **72.** In Carius method of estimation of halogen, 0.25 g of an organic compound gave 0.15 g of silver bromide (AgBr). The percentage of Bromine in the organic compound is  $\_\_\_ \times 10^{-1}\%$  (Nearest integer).

(Given: Molar mass of Ag is 108 and Br is  $80 \text{ g mol}^{-1}$ )

- **73.** Consider a complex reaction taking place in three steps with rate constants  $k_1, k_2$  and  $k_3$  respectively. The overall rate constant k is given by the expression  $k = \sqrt{\frac{k_1k_3}{k_2}}$ . If the activation energies of the three steps are 60, 30 and 10 kJ mol<sup>-1</sup> respectively, then the overall energy of activation in kJ mol<sup>-1</sup> is \_\_\_\_\_\_. (Nearest integer)
- **74.** The possible number of stereoisomers for 5-phenylpent-4-en-2-ol is \_\_\_\_\_.
- **75.** The observed and normal molar masses of compound  $MX_2$  are 65.6 and 164 respectively. The percent degree of ionisation of  $MX_2$  is \_\_\_\_\_\_. %, (Nearest integer)